

# The Predictive Information Content of External Imbalances for Exchange Rates Returns: How Much is It Worth?

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## ● Exchange Rate Predictability

- Economic fundamentals generally fail to outperform a naïve random walk model (Meese and Rogoff, *JIE*, 1983)
- Forecasting nominal exchange rate returns is a difficult exercise at short horizon (Mark, *AER*, 1995; Berkowitz and Giorgianni, *ReStat*, 1999)

## ● Disconnect Puzzle

- High persistent fundamentals and discount factor close to unity (Engel and West, *JPE*, 2005)
- Failure to capture parameter instability (Rossi, *IER*, 2005; Sarno and Valente, *JEEA*, 2009)
- Higher-order expectations and information heterogeneity (Bacchetta and van Wincoop, *AER*, 2006)

# International Financial Adjustment

- Gourinchas and Rey (2007) explore the implication of the intertemporal budget constraint

$$nxa_t \approx - \sum_{i=1}^{\infty} \rho^i E_t (r_{t+i} + \Delta nx_{t+i})$$

- $nxa_t$  is a linear combination of detrended components of exports, imports, external assets and liabilities
- $r_{t+1}$  is the real return on net foreign assets
- $\Delta nx_{t+1}$  is the detrended net export growth
- $\rho$  is the discount factor

$nxa_t$  must forecast either future portfolio returns  
or future net export growth, or both

- A measure of **cyclical external imbalances** incorporating information from the detrended trade balance and the foreign asset position

$$nxa_t \equiv |\mu^a| \epsilon_t^a - |\mu^l| \epsilon_t^l + |\mu^x| \epsilon_t^x - |\mu^m| \epsilon_t^m$$

- $\mu^a$  : average share of assets in the net foreign assets
- $\mu^x$  : average share of exports in the trade balance
- $\epsilon_t^l$  : stationary component of (log) liabilities to wealth ratio
- $\epsilon_t^m$  : stationary component of (log) imports to wealth ratio

*nxa<sub>t</sub>* rises with assets and exports and declines with imports and liabilities

# International Financial Adjustment (cont'd)

- Deteriorations in external imbalances ( $nx a_t < 0$ ) imply
  - future trade surpluses  $E_t \Delta n x_{t+1} > 0$  (**trade channel**)
  - high returns on the net foreign portfolio  $E_t r_{t+1} > 0$  (**valuation channel**)
- The exchange rate plays a critical role
  - today's imbalances contain valuable information about future exchange rate returns
  - $nx a$  contains out-of-sample forecasting power at all horizons between one and 16 quarters

- Extensive literature on statistical measures but not on the economic value criteria
  - Exchange rate volatility (West, Edison and Cho, *JIE*, 1993)
  - Long-horizon predictability (Abhyankar, Sarno and Valente, *JIE*, 2005)
  - Short-horizon predictability (Della Corte, Sarno and Tsiakas, *RFS*, 2009)
- Is the predictive information in  $nxa$  economically significant?
  - how does an investor exploit FX predictability?
  - can we construct a bilateral measure of  $nxa$ ?
- An economic assessment of the predictive ability of cyclical external imbalances both in-sample and out-of-sample

- Estimating the following predictive regression

$$\Delta_k s_{t+k}^{(i)} = \alpha + \beta nxa_t^{(i)} + \varepsilon_{t+k}$$

- $\Delta_k s_{t+k}^{(i)}$  : nominal exchange rate return between the US dollar and the currency  $i$
- $nxa_t^{(i)}$  : bilateral measure of cyclical external imbalances between the US and the foreign country  $i$
- Bilateral data on external assets and liabilities are not available and  $nxa_t^{(i)}$  is not directly observable

# Modeling FX Returns (cont'd)

- We estimate  $nxa_t^{(i)}$  using a IV estimator
  - regress the US global  $nxa_t$  on a set of instruments
  - use the fitted value as a proxy for  $nxa$
- Instruments
  - global  $nxa_t$  for the foreign country  $i$
  - detrended net exports  $nX_t^{(i)}$  between the US and the foreign economy  $i$

$$nX_t^{(i)} \equiv |\mu^{x^{(i)}}| \epsilon_t^{x^{(i)}} - |\mu^{m^{(i)}}| \epsilon_t^{m^{(i)}}$$

- **FX rates**

- quarterly data from *Datastream*: Mar 1973 - Dec 2004
- bilateral US dollar exchange rates: GBP, EUR, JPY, and CAD

- **External Assets and Liabilities**

- aggregate annual data from Lane & Milesi-Ferretti (2007)
- aggregate quarterly data by linear interpolation and extrapolation

- **Exports and Imports**

- aggregate quarterly data from National Statistic Databases
- bilateral quarterly data the Bureau of Economic Analysis (BEA)

- **Net Worth**

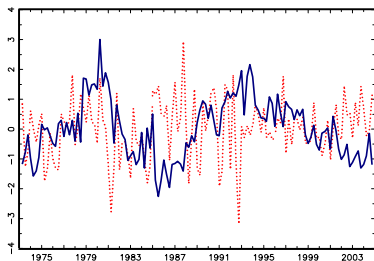
- aggregate annual data from National Statistic Databases
- aggregate quarterly data by linear interpolation and extrapolation

# Predictive Regression

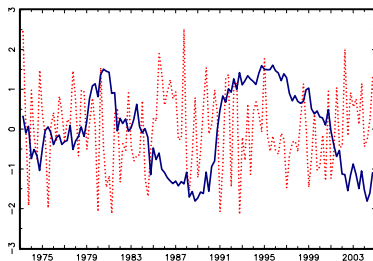
$k$	1	2	3	4	8	12	16
	<i>USD/GBP</i>						
$\beta/k$	-0.045 (-0.146, 0.111)	-0.034 (-0.129, 0.112)	-0.047 (-0.131, 0.075)	-0.048 (-0.130, 0.084)	-0.055 (-0.141, 0.054)	-0.060* (-0.150, 0.015)	-0.074** (-0.158, -0.009)
$R^2$	0.01	0.01	0.01	0.02	0.03	0.06	0.15
	<i>USD/EUR</i>						
$\beta/k$	-0.134*** (-0.262, -0.052)	-0.128*** (-0.246, -0.049)	-0.127*** (-0.243, -0.048)	-0.128*** (-0.255, -0.054)	-0.113*** (-0.212, -0.049)	-0.063*** (-0.170, -0.041)	-0.058*** (-0.151, -0.035)
$R^2$	0.06	0.11	0.18	0.22	0.28	0.28	0.32
	<i>USD/JPY</i>						
$\beta/k$	-0.178*** (-0.300, -0.073)	-0.172*** (-0.271, -0.070)	-0.154** (-0.225, -0.044)	-0.142** (-0.207, -0.019)	-0.107* (-0.1734, 0.010)	-0.059 (-0.128, 0.045)	-0.035 (-0.094, 0.042)
$R^2$	0.09	0.14	0.18	0.20	0.22	0.11	0.06
	<i>USD/CAD</i>						
$\beta/k$	-0.007 (-0.039, 0.062)	-0.022 (-0.054, 0.038)	-0.022 (-0.049, 0.034)	-0.027 (-0.049, 0.025)	-0.040** (-0.058, -0.002)	-0.037** (-0.055, -0.001)	-0.030* (-0.047, 0.001)
$R^2$	0.02	0.02	0.03	0.05	0.20	0.28	0.30

# Exchange Rate Returns and Bilateral Cyclical Imbalances

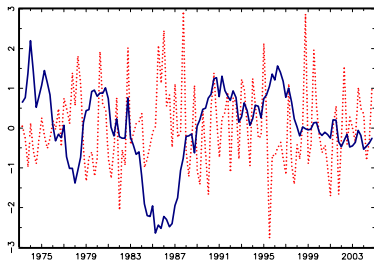
GBP



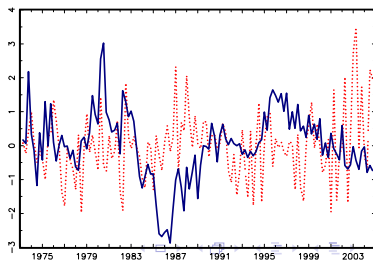
EUR



JPY



CAD



## • Objective

- Assess the economic value of exchange rate predictability in the context of dynamic asset allocation strategies

## • Framework

- Mean-variance analysis for the optimal portfolio choice of risk-averse investors
- West, Edison & Cho (*JIE*, 1993), Fleming, Kirby & Ostdiek (*JF*, 2001), Marquering & Verbeek (*JFQA*, 2004), Han (*RFS*, 2006), Della Corte, Sarno & Thornton (*JFE*, 2008), Della Corte, Sarno & Tsiakas (*RFS*, 2009)

## • Question

- How much would a risk-averse investor be willing to pay to **switch** from a portfolio strategy based on the Random Walk model to one that exploits the predictive information in  $nxa$ ?

# Maximum Return Strategy

- Maximize expected portfolio return subject to a target portfolio volatility:

$$\begin{aligned} \max_{w_t} \quad & w_t' \mu_{t+1|t} + (1 - w_t' l) r_f \\ \text{s.t.} \quad & (\sigma_p^*)^2 = w_t' \Sigma_{t+1|t} w_t \end{aligned}$$

- Solution:

$$\begin{aligned} w_t &= \frac{\sigma_p^*}{\sqrt{C_t}} \Sigma_{t+1|t}^{-1} (\mu_{t+1|t} - lr_f) \\ C_t &= (\mu_{t+1|t} - lr_f)' \Sigma_{t+1|t}^{-1} (\mu_{t+1|t} - lr_f) \end{aligned}$$

- Each model specification delivers a set of

$$\mu_{t+1|t} = E_t[r_{t+1}] \quad \text{and} \quad \Sigma_{t+1|t} = E_t[(r_{t+1} - \mu_{t+1|t})(r_{t+1} - \mu_{t+1|t})']$$

## ● **Setting**

- Each quarter, a US investor allocates his wealth between the domestic bond (US), and 4 foreign bonds (Canada, Germany, Japan and UK)
- At the beginning of each period, the foreign bonds deliver a riskless return in local currency
- The only risk exposure is FX risk

## ● **Dynamic Rebalancing**

- At the end of each period, the investor estimates the model specification
- Conditioning on these estimates, he forecasts the one-period ahead conditional means and variance-covariances
- He dynamically rebalances his portfolio by computing new optimal portfolio weights for the maximum return strategy

- **Quadratic Utility**

$$U(W_{t+1}) = W_{t+1} - \frac{\lambda}{2} W_{t+1}^2 = W_t R_{p,t+1} - \frac{\lambda}{2} W_t^2 R_{p,t+1}^2$$

where

$$R_{p,t+1} = R_f + w_t' (R_t - R_f)$$

- **Average Realized Utility** (West, Edison & Cho, *JIE*, 1993)

- set the investor's RRA equals to a constant

$$RRA_t = \frac{\lambda W_t}{1 - \lambda W_t} = \delta$$

- expected utility generated by a given level of initial wealth

$$\bar{U}(\cdot) = \frac{W_0}{T} \sum_{t=0}^{T-1} \left\{ R_{p,t+1} - \frac{\delta}{2(1+\delta)} R_{p,t+1}^2 \right\}$$

# Utility-Based Performance Measure

- **Performance Fee** (Fleming, Kirby & Ostdiek, *JF*, 2001)

- Equate the average utilities for competing portfolios

$$\sum_{t=0}^{T-1} \left\{ (R_{p,t+1}^* - \Pi) - \frac{\delta}{2(1+\delta)} (R_{p,t+1}^* - \Phi)^2 \right\} = \sum_{t=0}^{T-1} \left\{ R_{p,t+1} - \frac{\delta}{2(1+\delta)} R_{p,t+1}^2 \right\}$$

- $R_{p,t+1}^*$  is the gross portfolio return constructed using the NXA strategy
- $R_{p,t+1}$  is gross portfolio return implied by the RW strategy
- $\Phi$  is the value that makes the investor indifferent between the two alternative strategies

$\Phi$  measures the maximum performance fee a risk-averse investor is willing to pay to switch from the RW to the NXA strategy

# Utility-Free Performance Measure

- **Manipulation-free performance measure** (Goetzmann, Ingersoll, Spiegel & Welch, *RFS*, 2007)

$$M(R_p) = \frac{1}{(1-\delta)} \ln \left\{ \sum_{t=0}^{T-1} \left( \frac{R_{p,t+1}}{R_f} \right)^{1-\delta} \right\}$$

- $M(R_p)$  is an estimate of the premium return after adjusting for risk
- We build on this criterion

$$\Theta = M(R_p^*) - M(R_p)$$

- $\Theta$  interpreted as the certainty equivalent return

The performance measure  $\Theta$  does not require the assumption of quadratic utility to rank portfolios

- **A Critical Factor**

- essential to assess the profitability of trading strategies
- difficult to determine (type of investor, different components, value of the transaction)

- **Break-even Transaction Cost** (Han, *RFS*, 2006)

- the proportional transaction cost,  $\tau^{be}$ , making an investor indifferent between competing strategies
- the transaction costs equal to a fixed proportion of the value traded in each bond

$$\tau \left| w_t - w_{t-1} \frac{(1 + r_t)}{(1 + r_p)} \right|$$

- the maximum level of transaction cost an investor is willing to pay

- In-sample and out-of-sample analysis
  - Target portfolio volatilities:  $\sigma_p^* = \{8\%, 10\%, 12\%\}$
  - Degree of Relative Risk Aversion:  $\delta = 6$
  - Performance measures:  $\Phi$  and  $\Theta$  in annualized basis points
  - Break-even transaction costs:  $\tau^{be}$  in quarterly basis points

- **In-Sample Period**

- March 1973 to December 2004

- **Out-of-Sample Period**

- March 1993 to December 2004
  - Rolling window of 20 years

$\sigma_p^*$	RW			NXA			$\Phi$	$\Theta$	$\tau^{be}$
	$\mu_p$	$\sigma_p$	$SR_p$	$\mu_p$	$\sigma_p$	$SR_p$			
	<b>In-Sample</b>								
8%	13.4	9.0	0.70	14.9	8.7	0.90	148	142	134
10%	15.0	11.1	0.71	16.9	10.7	0.91	185	177	137
12%	16.6	13.3	0.71	18.8	12.7	0.91	222	212	141
	<b>Out-of-Sample</b>								
8%	12.9	9.9	0.88	14.5	7.8	1.32	160	155	153
10%	15.1	12.3	0.88	17.1	9.7	1.32	200	192	164
12%	17.2	14.8	0.88	19.6	11.7	1.32	241	230	175

- **Small Sample Bias**

- The low number of observations might cause small sample bias in parameter estimates
- This estimation error would affect the portfolio weights leading to sub-optimal asset allocation
- The estimates are adjusted by generating 10,000 time series by means of block-bootstrap

# Economic Value and Small Sample Bias

$\sigma_p^*$	RW			NXA			$\Phi$	$\Theta$	$\tau^{be}$
	$\mu_p$	$\sigma_p$	$SR_p$	$\mu_p$	$\sigma_p$	$SR_p$			
	<b>In-Sample</b>								
8%	13.4	9.0	0.70	15.0	8.7	0.90	151	145	136
10%	15.0	11.1	0.71	16.9	10.8	0.91	189	181	139
12%	16.6	13.3	0.71	18.9	12.8	0.91	227	217	143
	<b>Out-of-Sample</b>								
8%	12.9	9.9	0.88	15.1	7.8	1.38	220	212	190
10%	15.1	12.3	0.88	17.8	9.8	1.39	275	267	203
12%	17.2	14.8	0.88	20.5	11.7	1.39	331	315	216

- We examine the impact of imposing **economically meaningful restrictions** (Campbell & Thomson, *RFS*, 2008)
- **Rest 1**
  - the model suggest a negative relation between  $\Delta s_{t+1}^{(i)}$  and  $nxa_t^{(i)}$
  - we set  $\hat{\beta}$  equals to zero when it is estimated with a positive sign
- **Rest 2**
  - a positive value of  $nxa_t^{(i)}$  should imply a negative forecast of  $\Delta s_{t+1}^{(i)}$
  - we set  $E_t(\Delta s_{t+1}^{(i)})$  equals to zero when it is sign is the same as  $nxa_t^{(i)}$
- **Rest 1&2**
  - both *Rest 1* and *Rest 2* are simultaneously imposed

# Economic Value and Economic Restrictions

$\sigma_p^*$	RW			NXA			$\Phi$	$\Theta$	$\tau^{be}$
	$\mu_p$	$\sigma_p$	$SR_p$	$\mu_p$	$\sigma_p$	$SR_p$			
				<b>Rest 1</b>					
8%	12.9	9.9	0.88	14.5	7.8	1.32	157	152	153
10%	15.1	12.3	0.88	17.0	9.7	1.32	197	189	164
12%	17.2	14.8	0.88	19.6	11.6	1.32	236	225	175
				<b>Rest 2</b>					
8%	12.9	9.9	0.88	15.4	8.8	1.28	253	244	132
10%	15.1	12.3	0.88	18.2	10.9	1.28	316	304	136
12%	17.2	14.8	0.88	21.0	13.1	1.28	380	362	140
				<b>Rest 1&amp;2</b>					
8%	12.9	9.9	0.88	15.4	8.8	1.28	250	241	131
10%	15.1	12.3	0.88	18.2	10.9	1.28	314	301	134
12%	17.2	14.8	0.88	21.0	13.1	1.28	375	358	138

- The data to construct the predictive variable might be available in 'real time'
- We lag  $nxa_t^{(i)}$  in the conditioning information set as

$$\Delta s_t = \alpha + \beta nxa_{t-Lag}^{(i)} + \varepsilon_t$$

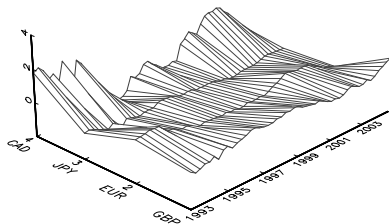
- the predictive variable is available with a given delay  $Lag$
- $Lag = 2$  (6-month time delay)
- $Lag = 4$  (1-year time delay)

# Economic Value in 'Real Time'

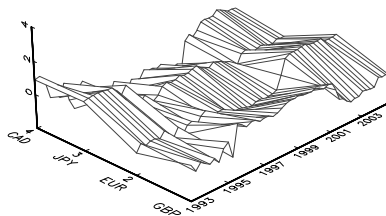
$\sigma_p^*$	$NXA_{Lag1}$			$NXA_{Lag2}$			$NXA_{Lag4}$		
	$\Phi$	$\Theta$	$\tau^{be}$	$\Phi$	$\Theta$	$\tau^{be}$	$\Phi$	$\Theta$	$\tau^{be}$
	<b>No Rest</b>								
8%	160	155	153	157	154	64	-93	-91	-
10%	200	192	164	197	191	66	-117	-113	-
12%	241	230	175	236	228	68	-140	-134	-
	<b>Rest 1</b>								
8%	157	152	153	166	162	70	-96	-93	-
10%	197	189	164	207	201	73	-120	-115	-
12%	236	225	175	249	240	75	-143	-137	-
	<b>Rest 2</b>								
8%	253	244	132	343	331	133	125	119	86
10%	316	304	136	429	411	136	156	148	92
12%	380	362	140	514	491	137	187	176	98
	<b>Rest 1&amp;2</b>								
8%	250	241	131	343	331	133	122	117	85
10%	314	301	134	429	411	136	153	145	91
12%	375	358	138	514	491	140	184	173	96

# Out-of-Sample Portfolio Weights

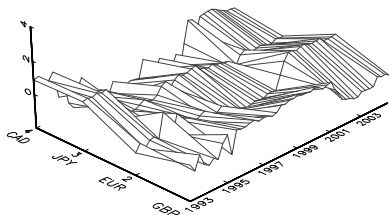
RW



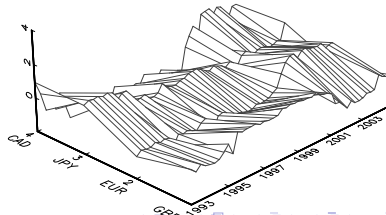
NXA



$NXA_{Rest1\&2}$



$NXA_{Lag2}$



- We extend Gourinchas and Rey (2007) by constructing bilateral measures of cyclical imbalances
- We use criteria of economic significance for exchange rate predictability
  - bilateral measures of external imbalances delivers substantial economic gains
  - impact of transaction costs, small sample bias and economic restrictions
- A promising result in the context of the empirical literature on exchange rate models and fundamentals